

$$\int \frac{1}{1+\sqrt{x}} dx = 2\sqrt{x} - 2\ln(\sqrt{x}+1) + c$$

$$\int_{-1}^8 \sqrt[3]{x} dx = \frac{45}{4}$$

$$\int \frac{dx}{x(1+2\sqrt{x}+\sqrt[3]{x})} = \frac{3}{4} \ln \frac{x\sqrt[3]{x}}{(1+\sqrt[3]{x})^2(\frac{1}{2}-\frac{1}{2}\sqrt[3]{x}+\sqrt[3]{x})^3} - \frac{3}{2\sqrt{7}} \operatorname{arctg} \left(\frac{4\sqrt[3]{x}-1}{\sqrt{7}} \right) + c$$

$$\int_0^\pi \sin x dx = 2$$

$$\int_{1/\sqrt{3}}^{\sqrt{3}} \frac{1}{1+x^2} dx = \frac{\pi}{6}$$

$$\int \frac{1}{\sqrt[3]{(x+1)^2(x-1)^4}} dx = -\frac{3}{2} \sqrt[3]{\frac{x+1}{x-1}} + c$$

$$\int_0^\pi x \sin x dx = \pi$$

Návod: použijte substituci $t = \sqrt{\frac{x+1}{x-1}}$

$$\int \cos x \cos 2x dx = \frac{1}{2} \sin x + \frac{1}{6} \sin 3x + c$$

$$\int_0^{\ln 2} \sqrt{e^x-1} dx = 2 - \frac{\pi}{2}$$

$$\int \cos x \cos 2x \cos 3x dx = \frac{x}{4} + \frac{\sin 2x}{8} + \frac{\sin 4x}{16} + \frac{\sin 6x}{24} + c$$

$$\int_{-1}^1 \frac{x}{\sqrt{5-4x}} dx = \frac{1}{6}$$

$$\int \frac{\sin^3 x}{\cos^4 x} dx = \frac{1}{3 \cos^3 x} - \frac{1}{\cos x} + c$$

$$\int_0^1 \frac{1}{x^2+x+1} dx = \frac{\pi}{3\sqrt{3}}$$

$$\int \cos^5 x dx = \sin x - \frac{2}{3} \sin^3 x + \frac{1}{5} \sin^5 x + c$$

$$\int_1^9 x\sqrt{1-x} dx = -\frac{468}{7} = -66\frac{6}{7}$$

$$\int \frac{\sin^2 x}{1+\sin^2 x} dx = x - \frac{1}{\sqrt{2}} \operatorname{arctg}(\sqrt{2} \operatorname{tg} x) + c$$

$$\int_1^e (x \ln x)^2 dx = \frac{5e^3-2}{27}$$

$$\int_0^\pi e^x \cos^2 x dx = \frac{e^\pi-1}{5}$$

$$\int \frac{1}{2\sin x - \cos x + 5} dx = \frac{1}{\sqrt{5}} \operatorname{arctg} \left(\frac{3\operatorname{tg} \frac{x}{2} + 1}{\sqrt{5}} \right) + c$$

$$\int \operatorname{tg}^3 x dx = \frac{1}{2} \frac{1}{\cos^2 x} + \ln |\cos x| + c$$

$$\int \sin^2 x dx = \frac{x}{2} - \frac{1}{4} \sin 2x + c$$

$$\int (x^2 - 2x + 2)e^{-x} dx = -e^{-x}(x^2 + 2) + c$$

$$\int x^2 e^{\sqrt{x}} dx = 2e^{\sqrt{x}}(x^2\sqrt{x} - 5x^2 + 20x\sqrt{x} - 60x + 120\sqrt{x} - 120) + c$$

$$\int \frac{1}{(1+e^x)^2} dx = x - \ln(e^x+1) + \frac{1}{1+e^x} + c$$

Určete obsah plochy omezený danými křivkami:

- a) $y = x^2, x + y = 2$ $S = \frac{9}{2}$
 b) $y = 2^x, y = 2, x = 0$ $S = 2 - \frac{1}{\ln 2}$
 c) $y = x, y = x + \sin^2 x, 0 \leq x \leq \pi$ $S = \frac{1}{2}\pi$

Vypočítejte objem tělesa ohraničeného plochami, které vzniknou rotací daných křivek kolem osy x :

- a) $y = 2x - x^2, y = 0$ $S = \frac{16}{15}\pi$
 b) $y = e^{-x}\sqrt{\sin x}, 0 \leq x \leq \pi$ $S = \frac{\pi}{5}(e^{-2\pi} + 1)$

Ověřte, že délka křivky $y = \ln(1-x^2)$ v intervalu $[-\frac{1}{2}, \frac{1}{2}]$ je $L = -1 + 2\ln 3$